Structure-preserved machine learning for computational modeling

First-principle modeling and simulation of complex systems based on partial differential equations (PDEs) and numerical discretization have been developed for decades and achieved great success. Nonetheless, traditional numerical solvers face significant challenges in many practical scenarios, e.g., inverse problems, uncertainty quantification, design, and optimizations. Moreover, for complex systems, the governing equations might not be fully known due to a lack of complete understanding of the underlying physics, for which a firstprincipled numerical solver cannot be built. Recent advances in data science. and machine learning, combined with the ever-increasing availability of high-fidelity simulation and measurement data, open up new opportunities for developing data-enabled computational mechanics models. Although the state-of-the-art machine/deep learning techniques hold great promise, there are still many challenges - e.g., requirement of "big data", the challenge in generalizability/extrapolibity, lack of interpretability/explainability, etc. On the other hand, there is often a richness of prior knowledge of the systems, including physical laws and phenomenological principles, which can be leveraged in this regard. Thus, there is an urgent need for fundamentally new and transformative machine learning techniques, closely grounded in physics, to address the aforementioned challenges in computational mechanics problems.

This talk will briefly discuss our recent developments of scientific machine learning for computational mechanics, focusing on several different aspects of how to bake physics-induced bias into machine/deep learning models for data-enabled predictive modeling. Specifically, the following topics will be covered: (1) PDE-structure preserved deep learning, where the neural network architectures are built by preserving mathematical structures of the (partially) known governing physics for predicting spatiotemporal dynamics, (2) physics-informed geometric deep learning for predictive modeling involving complex geometries and irregular domains.

Bio. Dr. Jian-Xun Wang is a tenure-track assistant professor of Aerospace and Mechanical Engineering at the University of Notre Dame. Dr. Wang completed his Ph.D. in Aerospace Engineering at Virginia Tech in 2017 and followed it with a one-year postdoctoral scholar appointment at the University of California, Berkeley before joining Notre Dame in 2018. Dr. Wang has a multidisciplinary research background, cutting cross scientific machine learning, data assimilation, Bayesian inference, uncertainty quantification, and computational mechanics. In particular, his research focus is at the interface of physics-informed deep learning, data-driven modeling, scientific computing, and physics-based computational mechanics. He has (co-) led research projects with \$5M funds sponsored by multiple agencies, including NSF, AFSOR, ONR, DARPA, CICP, etc. Dr. Wang received the NSF CAREER Award in 2021, the Top 10 Outstanding Chinese American Youth Award in 2022, ONR Young Investigator Award in 2023. Dr. Wang also serves on the editorial board of Nature Scientific Report, and he is a member-at-large of the US. Association of Computational Mechanics (USACM) Technical Thrust Area on Uncertainty Quantification.